

Design of compression members -

STEP-1 Find the effective length less. by given end conditions.

STEP-2 Assume suitable value of slenderness ratio

- (i) For single angle assume λ b/w 120 to 150
- (ii) For double angle 100 to 120
- (iii) For channel secⁿ 80 to 100
- (iv) For I section 60 to 90
- (v) For builtup secⁿ 30 to 50.

STEP-3 Select the value of σ_{ac} corresponding to assumed value of λ .

STEP-4 Compute gross area $A = \frac{P}{\sigma_{ac}}$

STEP-5 Choose a suitable secⁿ from steel tables having area computed in step-4.

STEP-6 Find r_{min} for secⁿ.

STEP-7 Compute slenderness ratio

$$\lambda = \frac{l_{eff}}{r_{min}}$$

if this matches with assumed value of λ then design is o.k. otherwise repeat steps 3 to 7.

See prob. P. 195. B. C. Punmia,

Compression members

Permissible compressive stress -

$$\sigma_{ac} = 0.6 f_y \frac{f_{cc} \cdot f_y}{[(f_{cc})^n + (f_y)^n]^{1/n}}$$

f_y = yield stress of steel.

f_{cc} = Elastic critical stress in compression

$$= \frac{\pi^2 E}{\lambda^2}$$

E = modulus of elasticity of steel = 2×10^5 MPa

λ = slenderness ratio = $\frac{l_{eff}}{r_{min}}$

h = a factor assumed as 1.4

Compressive strength

$$P = A \times \sigma_{ac}$$

Min radius of gyration

$$r_{min} = \sqrt{\frac{I_{min}}{A}}$$

I_{min} = min moment of inertia.

(Pb) A single angle strut ISA 50x50x6 mm of a roof truss is 1.06 m long. It is connected by one rivet at each end. Determine the safe load this strut can carry. ($f_y = 250$ MPa)

Sol.

For ISA 50x50x6 mm (from steel table)

$$A = 5.68 \text{ cm}^2$$

$$r_{min} = 0.96 \text{ cm}$$

~~least radius~~ For one rivet at each end $l_{eff} = 1.06 \text{ m}$

$$\lambda_{max} = \frac{l_{eff}}{r_{min}} = \frac{1.06 \times 100}{0.96} = 110.42$$

From steel table ($f_y = 250$ MPa, $\lambda = 110.42$)

$$\sigma_{ac} = 72 - \frac{(72-64)(110.42-110)}{(120-110)}$$

$$= 72 - \frac{8 \times 0.42}{10}$$

$$= 71.664 \text{ N/mm}^2$$

From steel table for single angle and each end connected by one rivet

$$\begin{aligned} \text{Per. compressive stress} &= 0.87 \sigma_{ac} \\ &= 0.87 \times 71.664 \\ &= 57.33 \text{ N/mm}^2 \end{aligned}$$

$$\sqrt{\frac{f_y}{2}} = \frac{\sqrt{f_y \cdot f_y}}{2.5}$$

So. ~~Per~~ safe load.

$$P = A \times \sigma_{ac}$$

$$= 5.68 \times 100 \times 57.33$$

$$= 32.56 \text{ kN}$$

- (P6) A discontinuous ~~discontinuous~~ strut 2.5 m long, consists of an angle ISA 100x75x8 mm ^{longer leg} connected with 10 mm thick gusset plate. Find strength of this compression member if
- each end connected by one rivet.
 - each end connected by two rivets
- ($f_y = 250 \text{ N/mm}^2$)

Sol. For ISA 100x75x8 mm
 $A = 1336 \text{ mm}^2$
 $r_{\min} = 15.9 \text{ mm}$.

For one rivet at each end

$$l_{\text{eff}} = 2.5 \text{ m}$$

$$\lambda = \frac{l_{\text{eff}}}{r_{\min}} = \frac{2.5 \times 1000}{15.9} = 157.23$$

From steel table ($f_y = 250 \text{ N/mm}^2$, $\lambda = 157.23$)

$$\begin{aligned} \sigma_{ac} &= 45 - \frac{(45-41)(157.23-150)}{160-150} \\ &= 42.11 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \text{Per. compressive stress} &= 0.8 \times \sigma_{ac} \\ &= 0.8 \times 42.11 \\ &= 33.69 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \text{Strength of member} \\ P &= A \times \sigma_{ac} \\ &= 1336 \times 33.69 \\ &= 45 \text{ kN.} \end{aligned}$$

For Two rivets at each end -

$$\begin{aligned} l_{\text{eff}} &= 0.85L \\ &= 0.85 \times 2.5 \\ &= 2.125 \text{ m.} \end{aligned}$$

$$\lambda = \frac{l_{\text{eff}}}{r_{\min}} = \frac{2.125 \times 1000}{15.9} = 133.65$$

From steel table ($f_y = 250 \text{ N/mm}^2$, $\lambda = 133.65$)

$$\begin{aligned} \sigma_{ac} &= 57 - \frac{(57-51)(133.65-130)}{140-130} \\ &= 54.81 \text{ N/mm}^2 \end{aligned}$$

$$\text{Per. compress stress} = 54.81 \text{ N/mm}^2$$

$$\begin{aligned} \therefore \text{Strength of member} &= A \times \sigma_{ac} \\ &= 1336 \times 54.81 \\ &= 73.23 \text{ kN.} \end{aligned}$$